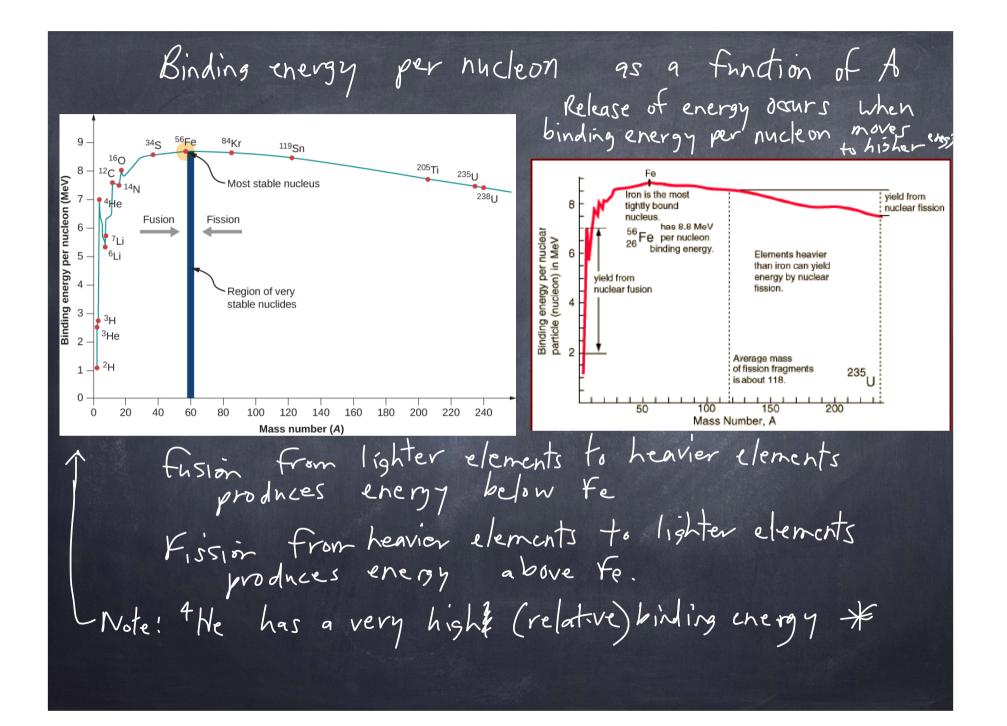
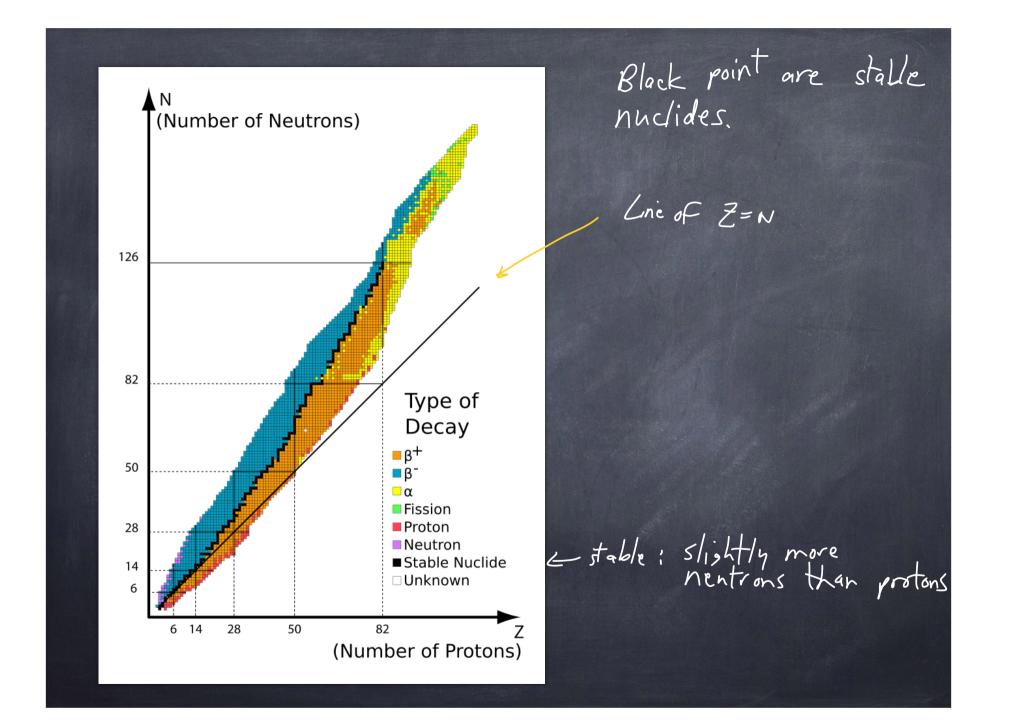
## PHY127 FS2024

Prof. Ben Kilminster Lecture 13 May 31st, 2024

Last time (Lecture 12); Nuclear binding = Z(mpc) + N(mnc) - mc energy m: mass of proton mass of the m: mass of neutron nucleus. This binding chergy is about 12 of the mass  $\frac{8 \text{ MeV}}{1 \text{ M}} = \frac{8 \text{ MeV}}{930 \text{ MeV}} \sim 12$ 





Nuclides with 
$$Z \cong N$$
 tend to have lower energies  
t be more stable.  
Atoms are more stable when electron shells  
 $(s, p, d, ...)$  are filled  $\rightarrow$  "closed shells"  
Also true for nuclei with "magic" numbers  
of nucleons:  $Z, 8, 20, 78, ...$   
 $(Ayplies to both protons + neutrons separately)$   
For instance,  $\frac{4}{2}Ne(Z=2, N=2)$   
is "doubly magic"  $\rightarrow$  extremely stable  
Nelium  
 $Melium$   
 $Melium$   
 $Melium$   
 $Melium$   
 $Melium$ 

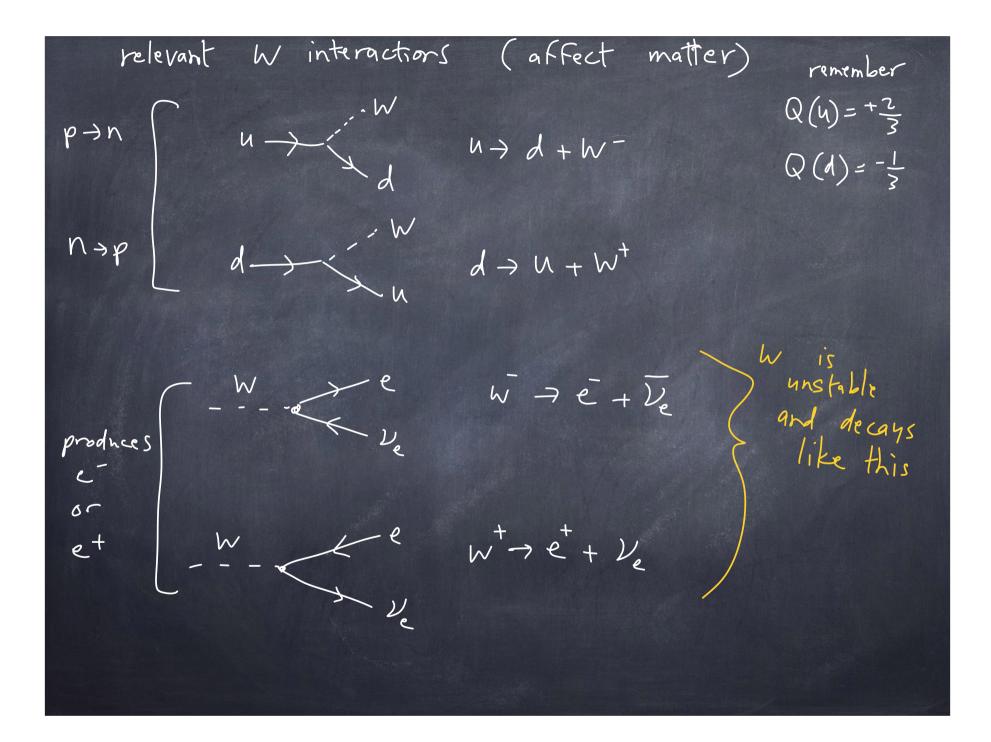
Often, E also decays by X decay, causing 9 Succession of & decays. Unstable Nuclides with A=4n, 4n+1, 4n+2,... (where n is an integer) typically exhibit multiple & decays. 232 90 1.41e+10 Years 228**Th** α 228 Ra 228 Ra 228 Ra 5.7 Years 24 Ra 3.6 Days Radium For instance, 232 Th. Francium 220 **Rn** (4.58 = 232)Rador We see 232 th decays by demission to 228 Rg. Later 20Th Astatine 6 PO Poloniur Bismuth decays to 228 Ra, ... many & decays happen. Alkali Metals Alkaline Earth M

what is a neutrino? Symbol: 2 (nu) It is a neutral lepton, like the electron but with no electric charge. It only interacts through the weak nuclear interaction. A lead tube one lightyear long (9 trillion km) would only stop 1/2 of (9 E12 km) nentrinos. wow

Sources of neutrinos: radioactive decays
nentrinos produced in sun (from Fusion) nentrinos produced in nuclear reactors (fission)
 nentrinos produced in accelerators 10" neutrinos from the sun travel through each of your / Fingernails each second. That's a lot! Detecting neutrinos: Super-Kamiokande: 50 kilotonnes of water T 42m 1-39m All of this water causes about 4000 neutrinos from sun to interact. Not so many!

weak nuclear force  

$$n \rightarrow p^{\dagger} + e^{\dagger} + k^{\dagger}$$
  
W is a force carrier  
for the weak force.  
 $d \Rightarrow u + e^{\dagger} + k^{\dagger}$ 
  
 $d \Rightarrow u + e^{\dagger} + k^{\dagger}$ 
  
 $for the meak force.$   
 $for the force.$   
 $for the meak forc.$ 



so a 
$$p \neq n + e^{\pm} + v_e$$
  
But protons are stable by themselves  
but can decay inside a nucleus  
Free neutrons decay into a proton  $t \neq t = v_e$   
in ~15 minutes  
Neutrinos were hypothesized because it was  
found that  $n \Rightarrow p \pm e^{\pm}$   
odoesn't conserve energy  
(so we need a neutrino)  
postron  $a \equiv e^{\pm} = e^{\pm} + e^{\pm} + e^{\pm} + v_e$   
electron  $A \equiv e^{\pm} = e^{\pm} + e^{\pm} + e^{\pm} + v_e$ 

& radiation (genna) Occurs when a nucleus makes a downward transition from one energy to a lower energy level (like in atoms). But nuclear transitions produce higher energy photons than atomic transitions (millions of times larger) J: used in medical applications (imaging) + radiation therapy. I process happens when a nuclei is left in an excited state folloning a X or B decay Ame A E + of Z E + of also written  $z \in \rightarrow z \in +z$ 

Nalf-life of unstable nuclei:  

$$N(t) = N_0 e^{-2t}$$
 indecay constant  
 $N(t) = N_0 e^{-2t}$  initial number  
 $T_{adio} = t_{ve}$   
 $N(t) : # of particles$   
 $N(t) : # of particles$   
 $T_{\frac{1}{2}} = t_{\frac{1}{2}} = half-life$   
 $T_{\frac{1}{2}} = ln(2)$   
 $adivity = \Delta N = -2N$  (-) means N is  
decreasing  
This is explained more in next slides

Half-life principle:  
The number of decays in a short period of  
time aN is proportional to the time interval strand also  
to the number of particles, N.  
Therefore, the formula is:  
(AN=-2Nat)  
where 2 is the decay constant, which depends  
on the particular radioactive nuclide.  
The solution to this formula is solved with calculus:  
As 
$$\Delta t \rightarrow 0$$
, we use  $dt$ , and  $\Delta N \rightarrow dN$ .  
so  $dN = -2Ndt$   
Integrating,  $\int dN = \int -2dt \Rightarrow ln N = -2t + constant$   
(constant; and since, econstant; another constant, then  $\Rightarrow N = Ce^{2t}$ 

Half-life  

$$N(t) = N_0 e^{-\lambda t}$$

$$N(t) = N_0 e^{-\lambda t}$$

$$N_0: initial = of radioactive constant 
N_0: initial = of radioactive 
N(t): # of ptels after 
time t.
Now long does it take to decay half 
of the initial amount of isotope?
Initial = : N_0
$$T_{initial} = N_0 e^{-\lambda t} \qquad (what is t)$$

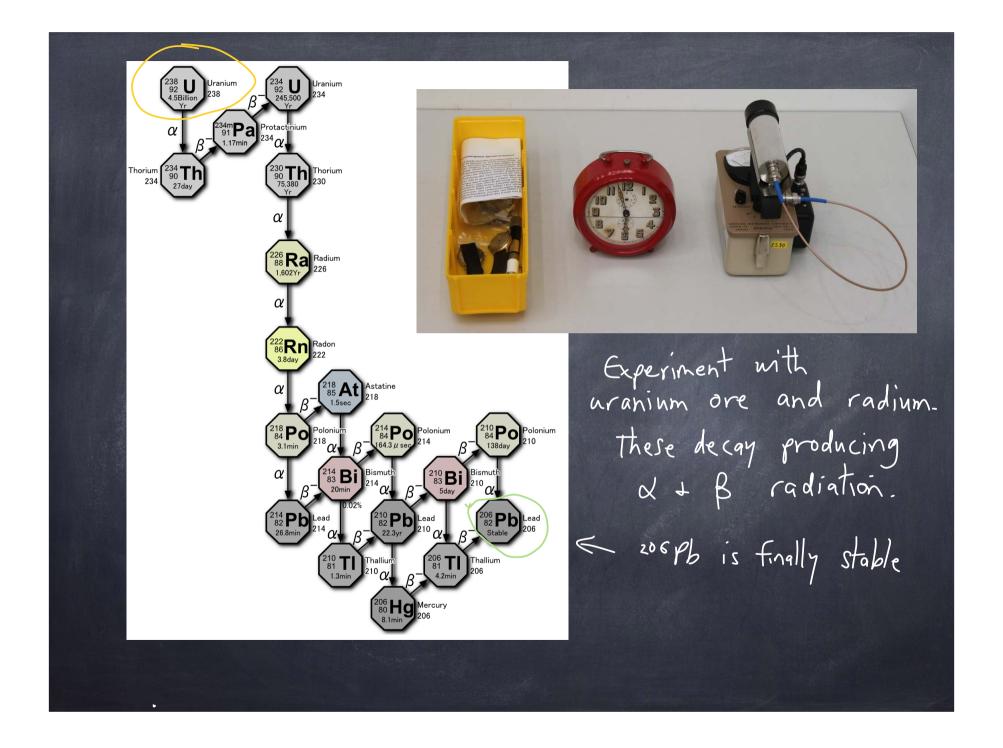
$$\frac{1}{2} = e^{-\lambda t}$$

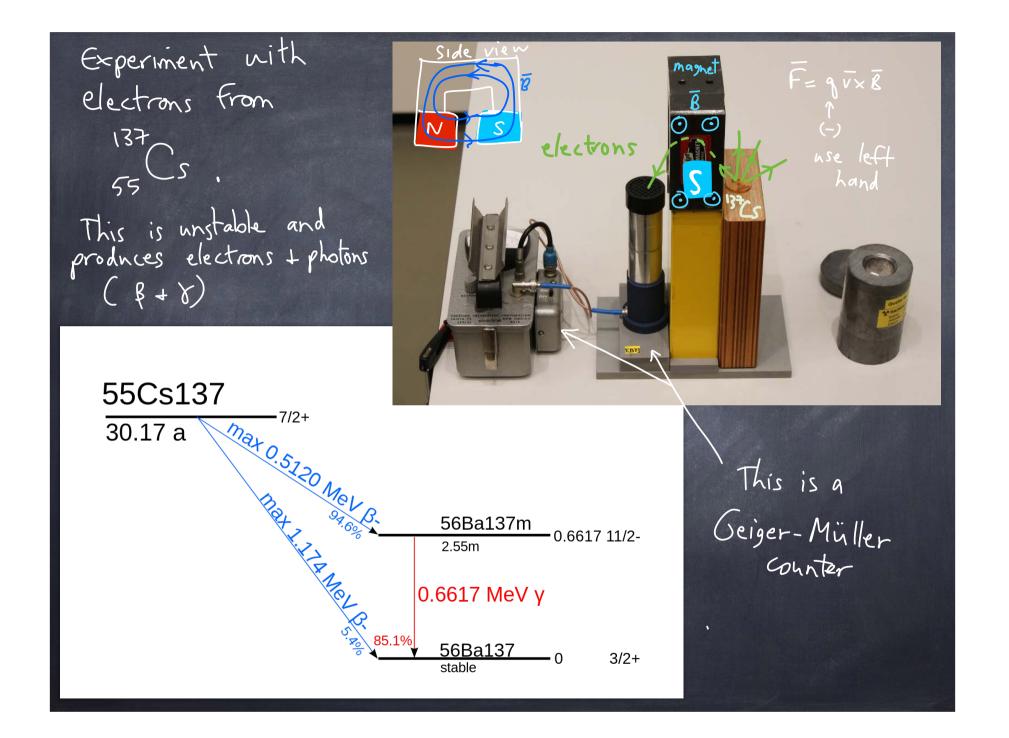
$$\log_2(\frac{1}{2}) = \ln \frac{1}{2} = \ln(e^{-\lambda t}) = -\lambda t$$

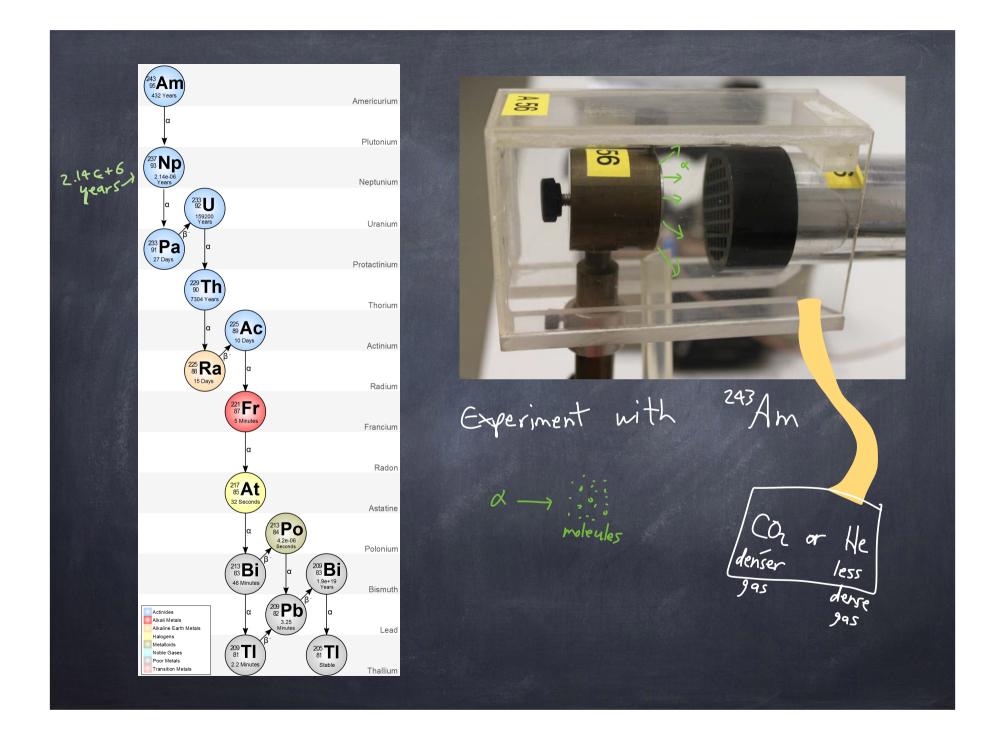
$$C_{\chi} = t_{\chi} = t = \frac{\ln(2)}{\lambda} = \frac{0.693}{\lambda} \quad half-life$$$$

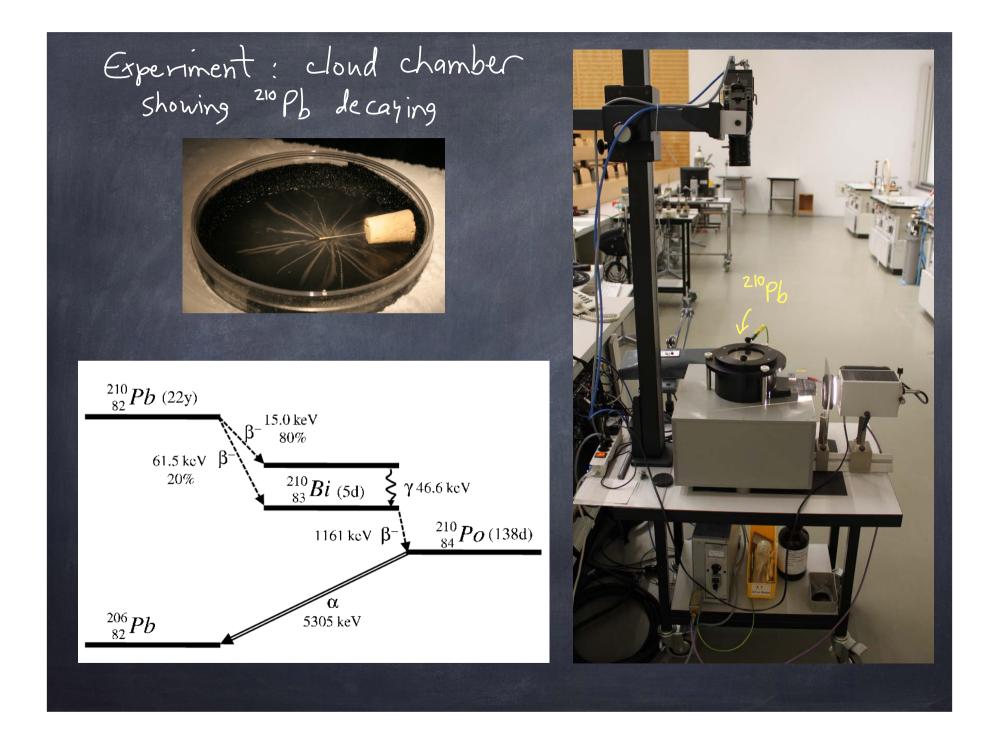
one half life :  $N_0 \rightarrow N_0/2$ two half-lives :  $N_0 \rightarrow N_0/4$ three -- :  $N_0 \rightarrow N_0/4$ 

Nuclide	Half-life	Type of change	Nuclide	Half-life	Type of change
rubidium-87	$5.7  imes 10^{10}$ years	beta	iron-59	45 days	beta
thorium-232	$1.39\times 10^{10} \text{ years}$	alpha	phosphorus-32	14.3 days	beta
uranium-238	$4.51 \times 10^9$ years	alpha	barium-131	11.6 days	electron capture and positron
uranium-235	$7.13  imes 10^9$ years	alpha	iodine-131	8.06 days	beta
plutonium-239	$2.44  imes 10^4$ years	alpha	radon-222	3.82 days	alpha
carbon-14	5730 years	beta	gold-198	2.70 days	beta
radium-226	1622 years	alpha	krypton-79	34.5 hours	electron capture and positron
cesium-133	30 years	beta	carbon-11	20.4 min	positron
strontium-90	29 years	beta	fluorine-17	66 s	positron
hydrogen-3	12.26 years	beta	polonium-213	$4.2  imes 10^{-6}  m s$	alpha
cobalt-60	5.26 years	beta	beryllium-8	$1  imes 10^{-16}  m s$	alpha





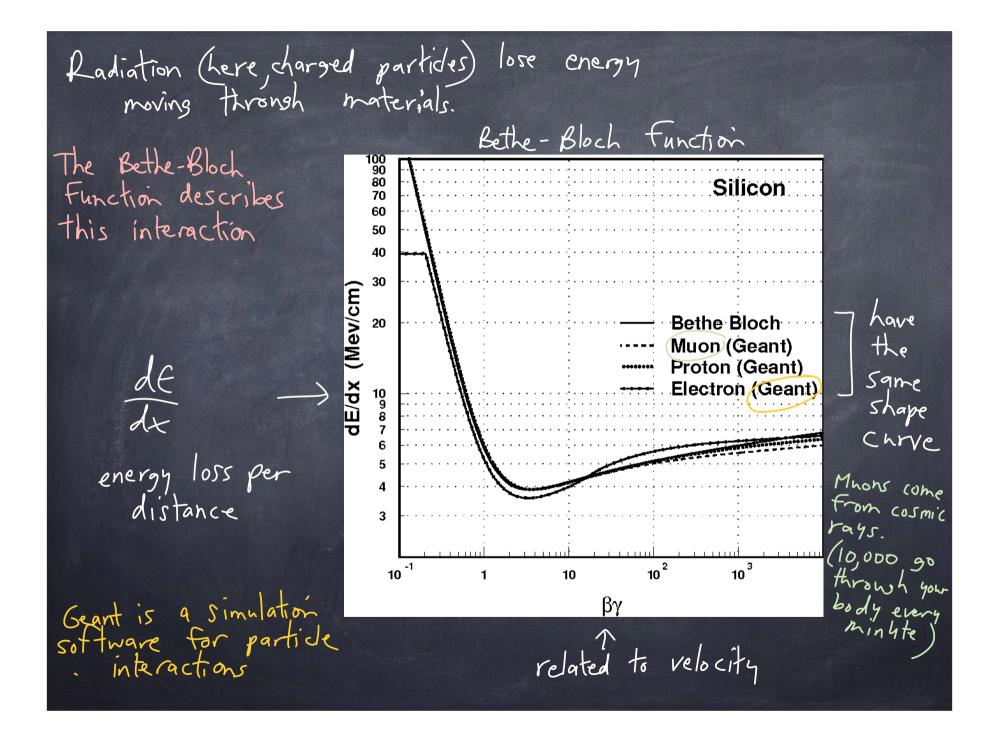


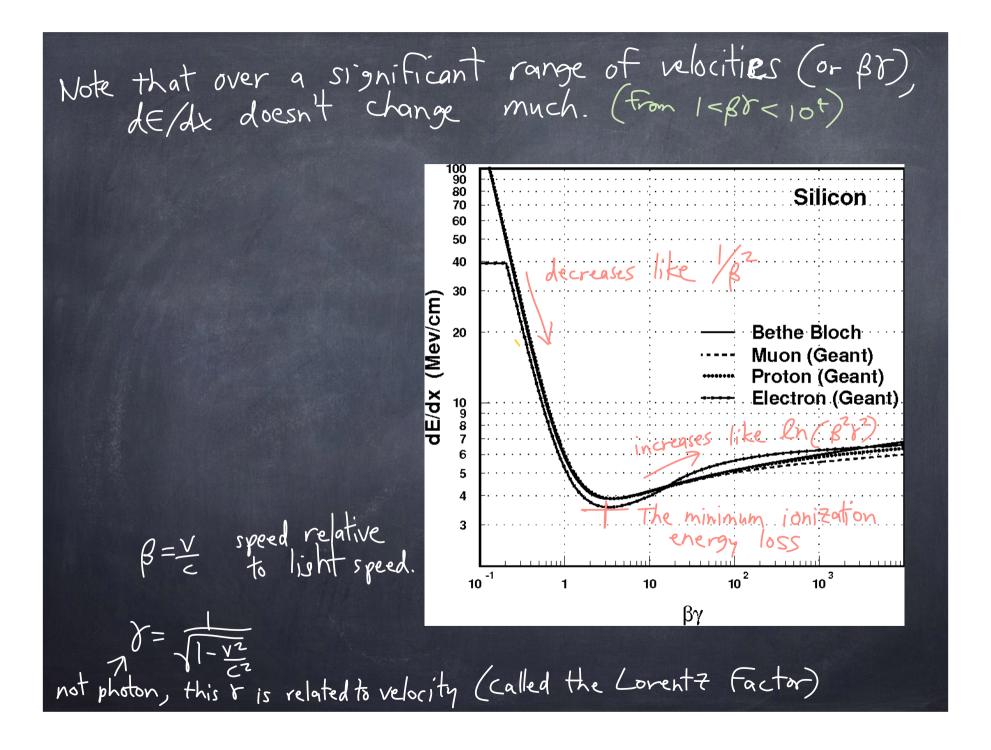


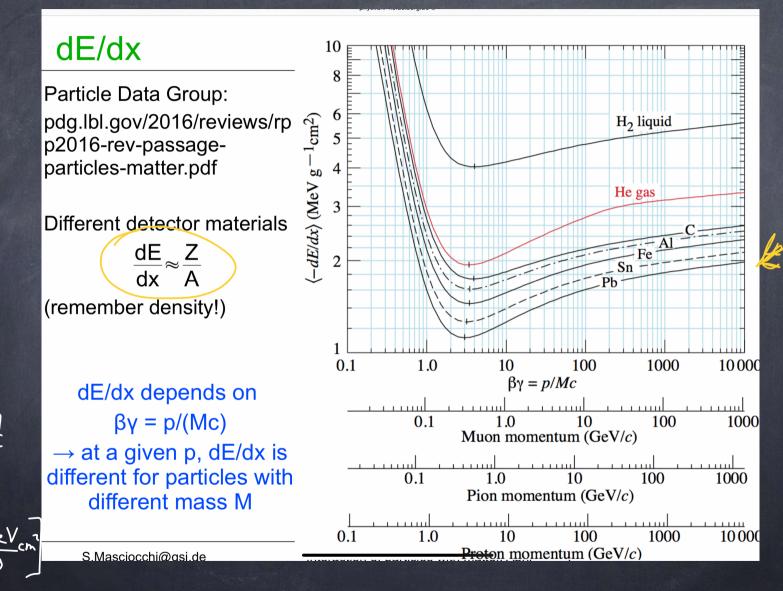
Some isotopes can reach equilibrium levels  
if they are produced by a long-lived parent and  
then decay thenself.  
Consider this case.  

$$N_{\rm eff}$$
  $3_{\rm e}$   $N_{\rm eff}$   $N_{\rm eff}$   
parent Ist daughter 2nd daughter  
The number of 1st daughter particles increases  
due to the parent decays, but also decreases  
due to its own decay to 2nd daughters.  
The number of Ni particles can therefore reach  
an equilibrium.  
The total change  
in AN in some  
time At

IF 7, is much smaller (Faster) than 20, then No(t) and Ni(t) are approximately constant in time. so equation 2 becomes  $\Delta N_{1}(t) = O = \left[ N_{0} \lambda_{0} - N_{1} \lambda_{1} \right] \Delta t$ Since  $\Delta t \neq 0$ ,  $N_0 2_0 = N_1 2_1$ and therefore, we can predict that the equilibrium number of N, daughters is N, = 20 No > The number of isotopes coming from long-lived parents is a constant and related to 20,2,,+No.







Here <u>dE</u> is <u>dx</u> <u>divided</u> by <u>density</u> of <u>material</u>

Me/

cm

## **Bethe-Bloch equation**

Considering quantum mechanical effects:

$$-\left\langle \frac{dE}{dx}\right\rangle = Kz^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2}\ln\frac{2m_e c^2 \beta^2 \gamma^2 T_{\text{max}}}{I^2} - \beta^2 - \frac{\delta(\beta^2 \gamma^2 T_{\text{max}})}{I^2} - \frac{\delta(\beta^2 \gamma^2 T_{\text{max}})}{I^2} - \beta^2 - \frac{\delta(\beta^2 \gamma^2 T_{\text{$$

. densitv

ρ

Validity:

 $.05 < \beta \gamma < 500$ 

GSI

11

 $M > m_{\mu}$ 

 $= 4\pi N_A r_e^2 m_e c^2 = 0.307 \text{ MeV } g^{-1} \text{ cm}^2$  $N_A = 6.022 \cdot 10^{23}$ Κ [Avogardo's number]  $T_{max} = 2m_e c^2 \beta^2 \gamma^2 / (1 + 2\gamma m_e / M + (m_e / M)^2)$  $r_e = e^2/4\pi\epsilon_0 m_e c^2 = 2.8 \text{ fm}$ [Max. energy transfer in single collision] [Classical electron radius]  $m_e = 511 \text{ keV}$ [Electron mass] Charge of incident particle Ζ Μ Mass of incident particle :  $\beta = v/C$ [Velocity]

Z : Charge number of medium

I : Mean excitation energy of medium

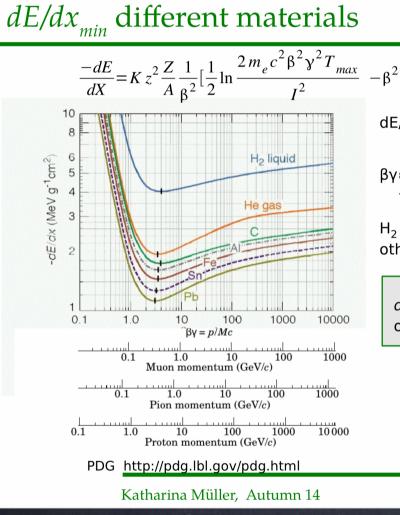
δ : Density correction [transv. extension of electric field]

S.Masciocchi@gsi.de

Interaction of particles with matter, April 27, 2017

 $= (1 - \beta^2)^{-2}$ 

[Lorentz factor]



$$-\beta^2 - \frac{\delta}{2} - \frac{C}{Z}$$
]

dE/dX depends on A, Z of target material

 $\beta \gamma \approx 3.5$  broad minimum  $\rightarrow$  minimum ionising particles (MIP)

 $\begin{array}{ll} H_2 & Z/A \cong 1 & dE/dX_{min} \cong 4 \ \text{MeV} \ /(g/cm^2) \\ \text{others} & Z/A \cong 0.5 & dE/dX_{min} \cong 2 \ \text{MeV} \ /(g/cm^2) \end{array}$ 

 $dE/dX_{min} \approx$  1-1.7 MeV /(g/cm<sup>2</sup>) only weak material dependence

15

what is most important in understanding radiation damage to tissue is the dose delivered at each depth. Lliving t.living - - - - y de ott.

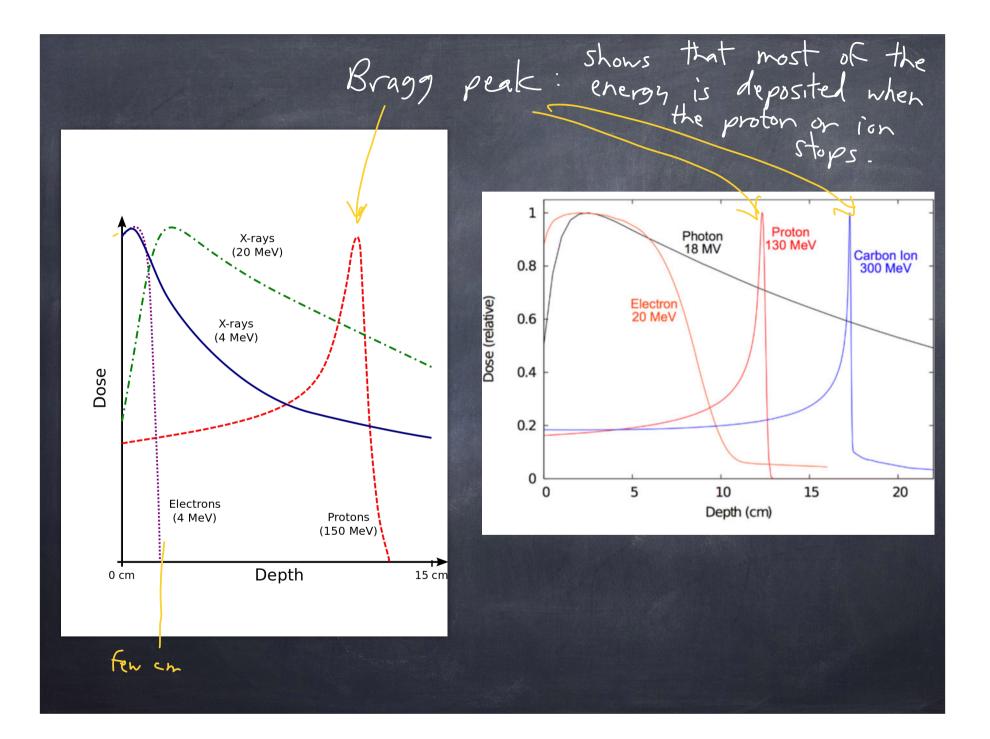
This depends on the type of radiation and its energy.

## TABLE 23.1

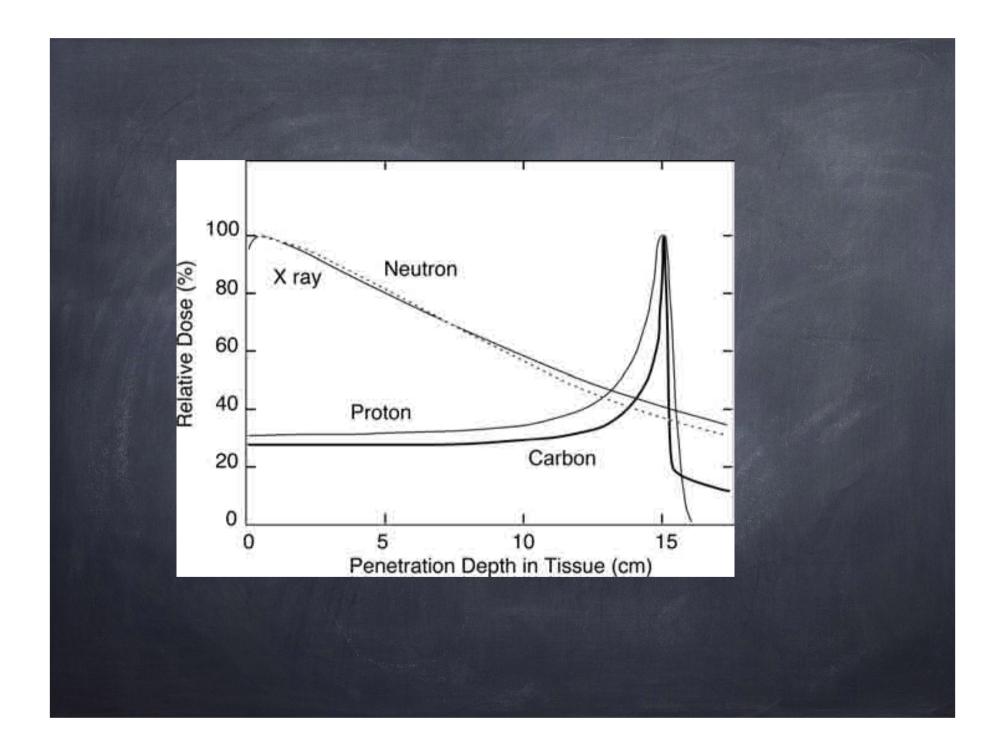
Range of various forms of radiation in biological tissue or water

Radiation type	Energy	Range
$\alpha$ -particles	5 MeV	40 µm
$\beta$ -radiation	20 keV	10 µm
$\beta$ -radiation	1 MeV	7 mm
$\gamma$ -radiation	20 keV	6.4 cm
$\gamma$ -radiation	1 MeV	65 cm
neutrons	1 MeV	20 cm

Range ? E how far the radiation Can travel before stopping



proton dose vs. depth for different energies. 1.2 PROTONS 250 MeV 50 MeV 225 NeV 100 MeV 130 MeV 180 MeV 200 MeV 11 0.3 -Relative dose 0.6 0.4 0.2 0 10 15 20 35 26 30 6 40 0 Depth in Water (cm) we can tune the energy of protons to deposit energy at a certain depth.



# Radiopharmacenticals

Incorporation of radioactive isotopes into cells or in organs of body allows radioactive tracing or radiolabeling of a particular molecule as it passes through an organism. For instance, hydrogen , H and , H (tritium) have the same chemistry, but tritium is radioactive  $(T_{\chi} = |Z \text{ years})$ :  $^{3}_{H} \rightarrow ^{3}_{Z} \text{He} + \bar{\nu}_{e}$ Since its lifetime is long, you wouldn't necessarily put it in a human body, but it could be used as a radiolabel for investigating hydrogen molecules in a sample. Also, electrons don't travel very far... So other radioactive nuclides are often used. (See next page)

### Radiation Applications Half-Life Radioisotope Most widely used \*6 h Technetium-99m Y SPECT brain imaging 13 h Iodine-123 Y $e^+$ PET 20 min Carbon-11 \*8.1 days Thyroid disorders $\beta, \gamma$ Iodine-131 \*14 days Large variety of uses in biology Phosphorus-32 β and medicine Heart imaging 74 h Thallium-201 Y Tumor imaging Gallium-67 78 h Y \*28 days Chromium-51 Red blood cell survival Y

# Table 26.4 Some Commonly Used Radioisotopes in Medicine

\*Produced in nuclear reactors; otherwise produced in an accelerator.



**International Patients Departments Stay Doctors & Sta** 

Department of Nuclear Medicine > About us > Center for Radiopharmacy (CRP)

## Center for Radiopharmacy (CRP)

The CRP is since 1993 the Swiss leading manufacturer of radioactive pharmaceuticals which are used in the nuclear medicine diagnostic by positron emission tomography (PET). These so-called PET-Tracers are molecules containing a very short lived radionuclide which decays by emission of positrons. Immediately after their manufacturing, they are intravenously administered to the patient and they rapidly distribute through the body. Because the radionuclides contained in PET-Tracers decay very fast, in most cases there will be no radioactivity left in the body after a few hours of their administration.

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### **Licensed products**

- <sup>18</sup>F-Fluoroglucose ZRP: Imaging of regional glucose consumption in cardiology, neurology and oncology
- <sup>18</sup>F-Fluorocholine ZRP: imaging of prostate or parathyroid cancer
- <sup>18</sup>F-Fluoethyltyrosine ZRP: Imaging of amino acid metabolism in the diagnosis of brain tumors
- <sup>18</sup>F-Sodium fluoride ZRP: Imaging of bone to detect abnormally altered bone formation activity
- <sup>18</sup>F-Vizamyl: Imaging of the density of neuritic β-amyloid plaques in the brain of adult patients with cognitive impairment who are being evaluated for Alzheimer's disease

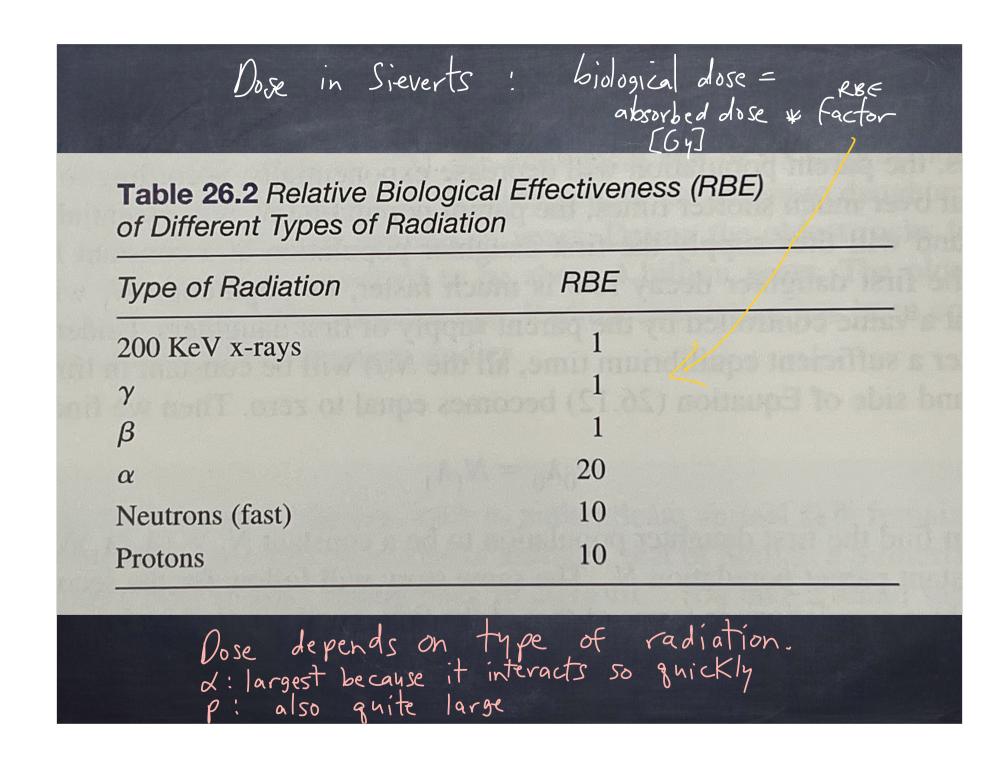
### Non licensed

- <sup>13</sup>N-ammonia: Imaging of myocardial perfusion
- <sup>15</sup>O-Water: Imaging of regional brain perfusion
- <sup>68</sup>Ga-DOTATATE ZRP: Imaging of neuroendocrine tumors with somatostatin receptors
- <sup>68</sup>Ga-PSMA 11: Imaging of prostate cancer
- <sup>18</sup>F-PSMA 1007 ZRP: Imaging of prostate cancer

Table	26.3	Typical	Human	Radiation	Doses
-------	------	---------	-------	-----------	-------

.

Source	Annual Dose (Sv)	
Cosmic rays	$4 \times 10^{-4}$	
Cosmic rays (in high altitude airplane)	$7 \times 10^{-6}$ Sv/h	
Radioactive ores (external exposure)	$6 \times 10^{-4}$	
Ingested materials (mainly potassium)	$2 \times 10^{-4}$	
Inhalation of radon	$2 \times 10^{-4}$	
Diagnostic x-rays	$7 \times 10^{-4}$	

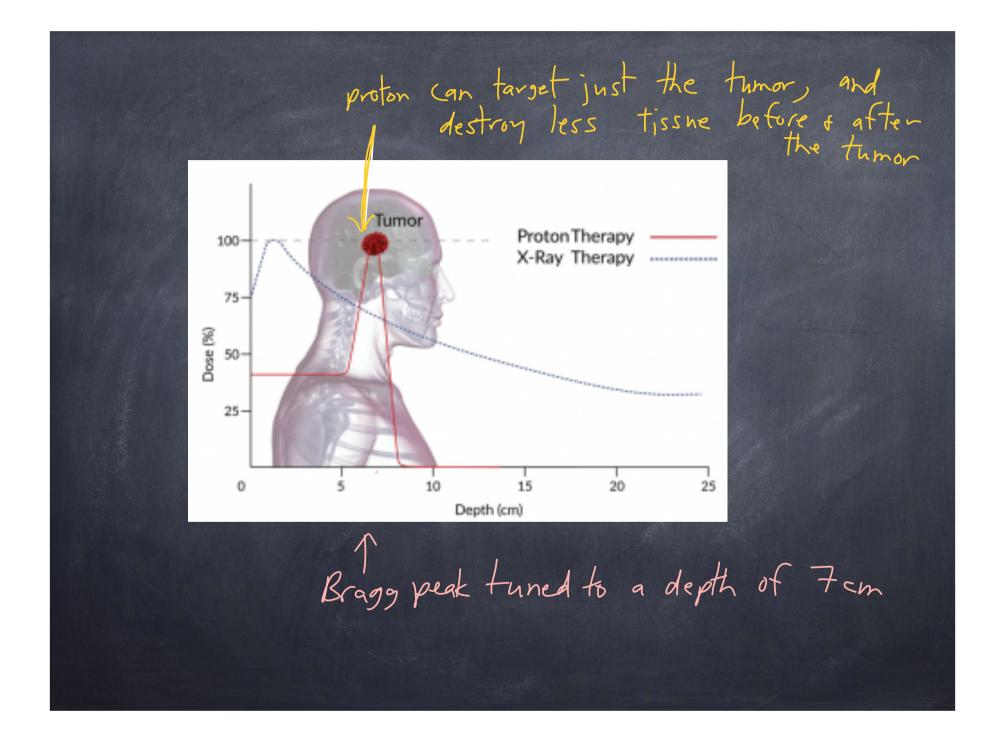


# Gamma therapy radiation

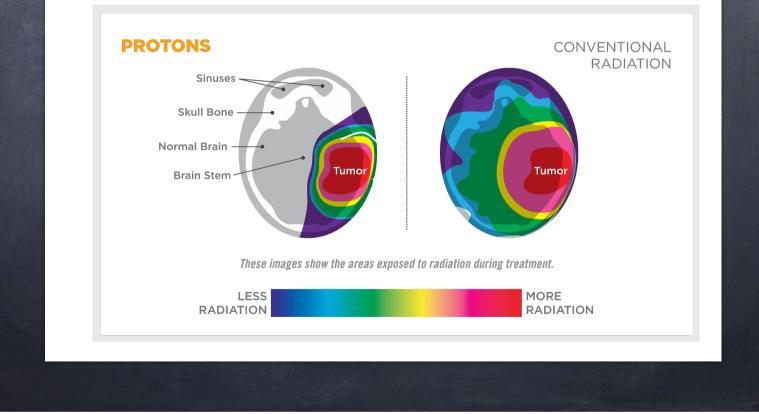


# Focused attention

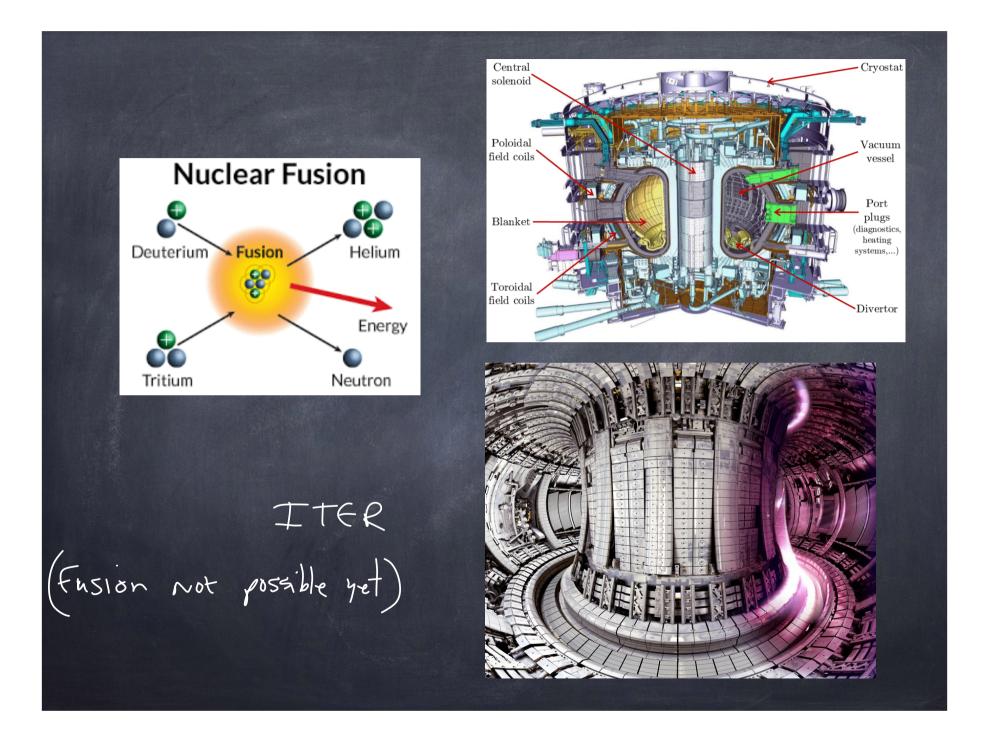
By attacking tumor from many angles, the intersection gets more dose, while heatty tissue damage is minimized.

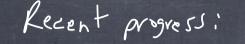






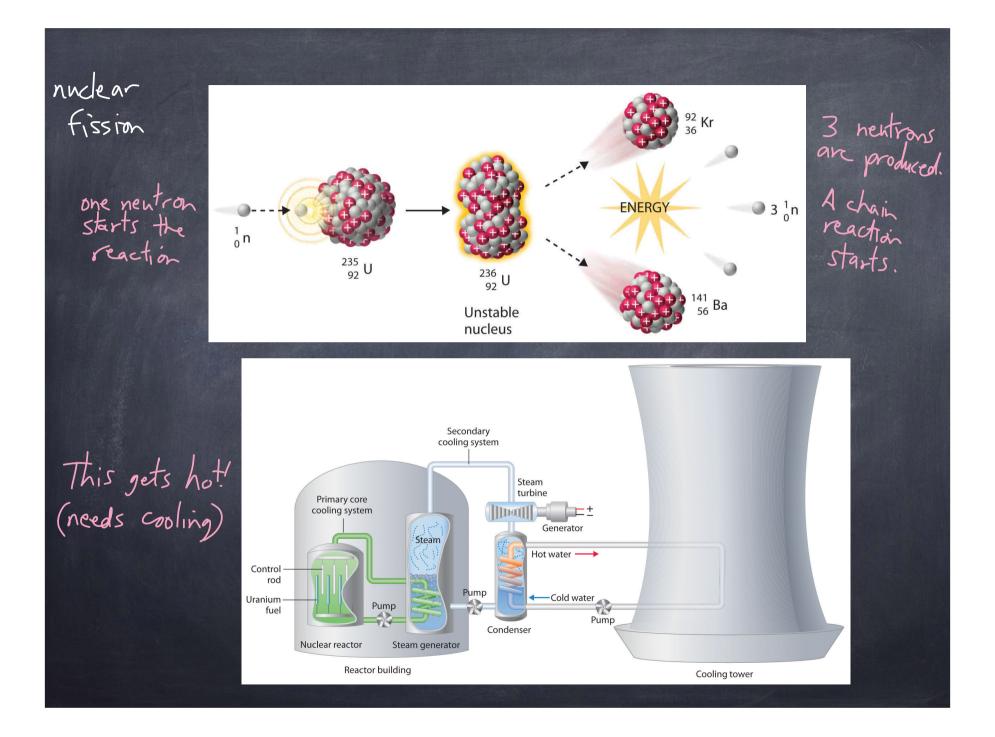






The US National Ignition Facility, which uses laser-driven inertial confinement fusion, was designed with a goal of break-even fusion; the first large-scale laser target experiments were performed in June 2009 and ignition experiments began in early 2011.[7][8] On 13 December 2022, the United States Department of Energy announced that on 5 December 2022, they had successfully accomplished break-even fusion, "delivering 2.05 megajoules (MJ) of energy output."[9]

Still a long time to go before commercial reactors possible, but this is a huge milestone.



### subcritical nuclear fission reactor can use nuclear waste as a fuel (Thorium) SWI swissinfo.ch Swiss perspectives in 10 languages Chinate change How a Swiss start-up X Q transmutex wants to reinvent Q All 🖪 News 😭 Images 📀 Maps 🕞 Videos : More Tools nuclear energy About 147 results (0.21 seconds) SwissInfo How a Swiss start-up wants to reinvent nuclear energy Transmutex is developing a new type of nuclear reactor that burns thorium instead of uranium. These power plants would be able to produce.. 30 Jan 2022 D Innovation Origins A Swiss company are developing a nuclear reactor powered I Transmutex's solution is the transmuter - a nuclear system activated by a particle accelerator. With it, they want to create nuclear power using... 14 Mar 2022 60 Heidi.news Transmutex peut-elle ressusciter le nucléaire suisse? Basé sur un accélérateur de particules et un matériau sous critique, le thorium la technologie de Transmutex évite le risque de perte de.. 6 Dec 2021 Le Temps L'émergence, à Genève, d'une énergie nucléaire presque ... Une entreprise genevoise, Transmutex, veut créer une centrale qui ne génère presque pas de déchets radioactifs et au fonctionnement sûr. 23 Dec 2021 ▲ Nuclear power generates about 10% of the electricity consumed in the world. Keystone / Giroscience / Science Photo No risk of meltdown because fission only happens when beam of particles is on. Transmuter aims to produce a proof of concept in ~ 25 years.

# principle of subcritical nuclear Fusion reactor proton beam keeps chain reaction going.

